## Mathematics

## Paper 3H (Calculator) <br> Higher Tier



| Surname | Other names |
| :--- | :--- |

## You should have:

A pen, pencil, ruler, eraser and a scientific calculator.
Tracing paper may be used.
A formula sheet.

## Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets.
- Answer all questions in the spaces provided - there may be more space than you need.
- You must show all your working.
- Diagrams are not accurately drawn, unless otherwise indicated.
- Check your answers if you have time at the end.

1 a) Expand and simplify $3(g+5)+7(g-2)$.
b) Factorise fully $5 x y+15 x$.

2 A box of 12 chocolate bars costs $£ 3.20$
Amir buys 96 chocolate bars.
How much does Amir spend?
$3 a=2.5$ and $b=-5$
a) Work out $4 a-b$.
b) Work out $b^{2}-\frac{1}{2} a$.

4 There are 18 giraffes and 24 elephants in a wildlife park.
a) Write the ratio of giraffes to elephants in its simplest integer form.
b) Write the ratio of elephants to giraffes in the form $1: n$.

5 The table shows the mass, in kilograms, of some dogs.

| Mass (kg) | Frequency |
| :---: | :---: |
| $0<m \leq 1$ | 4 |
| $1<m \leq 2$ | 6 |
| $2<m \leq 3$ | 17 |
| $3<m \leq 4$ | 10 |
| $4<m \leq 5$ | 13 |
| $5<m \leq 6$ | 23 |

Draw a frequency polygon to show this information.


6 An equilateral triangle has a base length of $(3 p-4) \mathrm{cm}$.

$(3 p-4) \mathrm{cm}$
a) Write an expression for the perimeter of the triangle.
b) The perimeter of the triangle is 141 cm .

Work out the value of $p$.

7 A cheetah runs 330 metres in 15 seconds.
a) Work out the cheetah's average speed.

Give your answer in metres per second (m/s).
$\qquad$ $\mathrm{m} / \mathrm{s}$
b) Convert your answer to part a) to kilometres per hour (km/h).
$\qquad$ km/h

A panther runs 100 metres in 11.5 seconds.
The time the panther takes is correct to 3 significant figures.
c) Work out the upper bound of the panther's speed, in metres per second, giving your answer correct to 3 significant figures.

8 The value of a car decreases by $15 \%$ in the first year after it is bought.
a) Miss Fisher buys a car for $£ 18000$

Find the value of Miss Fisher's car after one year.
b) One year after purchase, Mr Patel's car is worth $£ 17850$ How much did Mr Patel pay for the car?

9 The area of the trapezium is $40 \mathrm{~m}^{2}$
Work out the height, $h$, of the trapezium.


10 Work out the length of $A B$, giving your answer to 3 significant figures.


11 Rearrange $q=\frac{w^{3}}{2}-7$ to make $w$ the subject.

12 Here are some digit cards.


How many even numbers greater than 50000 can be made using these cards?

13 a) Simplify $\frac{2 t^{5} \times 9 t^{4}}{4 t^{3}}$
b) Annie writes $(2 x-3)^{2} \equiv 4 x^{2}-9$

Show that Annie is wrong.
c) Factorise $49-4 y^{2}$

14 Mrs Trent and Mr Khan set up a business.
Mrs Trent invests $£ 12600$ and Mr Khan invests $£ 7000$ The business makes $£ 23100$ profit. Mrs Trent and Mr Khan share the profit in the ratio of the amount they invested. How much of the profits does Mr Khan receive?
$15 \mathbf{a}=\binom{2}{-3}$ and $\mathbf{b}=\binom{4}{2}$
Write $\mathbf{4 a} \mathbf{+ 2 b}$ as a column vector.

16 The table and the histogram show information about the age of some office workers.

| Age (years) | Frequency |
| :---: | :---: |
| $16<a \leq 24$ | 12 |
| $24<a \leq 30$ | 15 |
| $30<a \leq 40$ | 33 |
| $40<a \leq 45$ |  |
| $45<a \leq 60$ | 15 |



Complete the table and the histogram.

17 The diagram shows a triangular prism.
$C D=15 \mathrm{~cm}$
$A D=20 \mathrm{~cm}$
Angle CDF $=42^{\circ}$


Calculate the size of the angle that line AF makes with the plane ABCD.
Give your answer correct to 3 significant figures.

18 The number of fish in a large lake $t$ years from now is $P_{t}$, where
$P_{0}=600000$
$P_{t+1}=1.02\left(P_{t}-5000\right)$
a) Work out the number of fish in the lake three years from now.

In a second lake, the number of fish is decreasing by $8 \%$ every year.
b) Which graph represents how the number of fish in the second lake changes over time?





c) At the start of 2022, there were 100000 fish in the second lake. How many fish will there be in the second lake at the start of 2025?
$19 \mathrm{~A}, \mathrm{~B}$ and C are points on the circumference of a circle, centre O .
DCE is a tangent to the circle.
$B C$ is parallel to FG .
Angle AFG $=62^{\circ}$
Angle $\mathrm{ACB}=71^{\circ}$
Angle $\mathrm{BCE}=x^{\circ}$
Find the value of $x$. Give reasons for each stage of your working.


20 The line $A B$ passes through the points $(1,2)$ and $(p, 17)$.
The gradient of the line $A B$ is 5
Work out the value of $p$.

21 The area of the shaded triangle in the rectangle is $x^{2}+4 x$.


Find the fraction of the rectangle that is shaded, giving your answer in its simplest form. You must show your working.

22 There are $n$ counters in a bag. 3 of the counters are red.

Two counters are taken from the bag.
Find, in terms of $n$, the probability that both counters are red.

23 Solve the simultaneous equations.

$$
\begin{gathered}
x^{2}+y^{2}=29 \\
x-y=3
\end{gathered}
$$

$x=$

$$
y=
$$

$\qquad$

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